

# Minimal Sampling Strategy to Estimate the Terminal Elimination Rate Constant

**Presenting Author:** Elie Sarraf<sup>1</sup>

**Co-Authors:** Donald M. Mathews<sup>1</sup>

<sup>1</sup>University of Vermont College of Medicine, Burlington, Vermont

**Introduction:** Methadone is a long acting opioid with NMDA receptor antagonist properties which has been commonly used for both chronic pain and as a drug detoxification for opioid abuse. Methadone induction is a clinical challenge due to its long and variable half-life [1-4] thus requiring many days to achieve steady state. In a separate abstract we describe an optimal methadone induction strategy by identifying the terminal elimination rate constant ( $\beta$ ) of the patient using a small initial dose followed by a dosing strategy using the accumulation index. We seek to determine the error of estimating  $\beta$  using a minimal sampling strategy that can be performed routinely on an outpatient basis and measure the impact of the error on this induction strategy.

**Methods:** Using Matlab (R2017b), we simulated the blood levels of 1,000,000 patients after a single test dose of methadone. The value of  $T_{1/2\alpha}$  and  $T_{1/2\beta}$  were randomly generated using a uniform random distribution with values between 1.5 and 4.2 hours and 8.5 and 120 hours respectively. The blood levels were sampled after the test dose of methadone. 3%, 4%, 5% and 7% coefficient of variation error was added to the sampled values.  $\beta$  was calculated in one of two manners:

- 1) Using the two samples and direct computation:

$$\beta = \frac{\ln(C(t_1)) - \ln(C(t_2))}{t_2 - t_1}$$

With  $C(t)$  being the measured plasma concentration at time  $t$ .

This method was applied to measurements that were sampled at a) 24 and 48 hours, and b) 24 and 72 hours.

- 2) Three samples collected at 24, 48 and 120 hours were used to identify the parameters  $B$  and  $\beta$  in the equation  $C_e(t) = B e^{-\beta t}$  such that it would minimize the following equation:

$$f(B, \beta) = \sum_i \left( \frac{C_e(t_i) - C(t_i)}{C_e(t_i)} \right)^2$$

Once the value of  $\beta$  was estimated, the optimal daily dosing strategy was applied to those simulated patients to determine the time for the methadone trough to be within 10% of the steady state trough (time to convergence). Also determined were the values of  $\beta$  that had a non-zero probability of having a 50% overshoot.

**Results:** Figure 1 shows the residual error plot between actual and the estimated values of  $\beta$ . Table 1 shows the mean and standard deviation of the residuals. The impact of the estimated  $\beta$  on the final time to convergence is shown in Figure 2. Table 2 shows the maximum  $T_{1/2}\beta$  estimates that would ensure 0% probability of greater than 50% overshoot, while values above those listed in the table would have a progressively increasing risk of overshoot.

**Discussion:** As would be expected, one can improve the  $\beta$  estimates by increasing the number of samples collected, increasing the delay between samples and using a laboratory device that provides more precise measurements. Given that the vast majority of real patient  $T_{1/2}\beta$  values of methadone are below 60 hours ( $\beta = 0.011/\text{hr}$ ) [1-4], one can effectively generate a minimal simple dosing strategy provided one has a well characterized laboratory device. This analysis will allow clinicians to have an appropriate margin of safety when dosing methadone through the optimal methadone induction strategy.

## References

1. Nilsson MI et al. Acta Anaesthesiol Scand Suppl. 1982;74: 66-69
2. Meresaar U et al. Eur J Clin Pharmacol. 1981; 20(6): 473-478
3. Wolff K et al. Eur J Clin Pharmacol. 1993; 44(2): 189-194
4. de Vos JW et al. Eur J Clin Pharmacol. 1995; 48(5):361-6.

## Figures and Tables

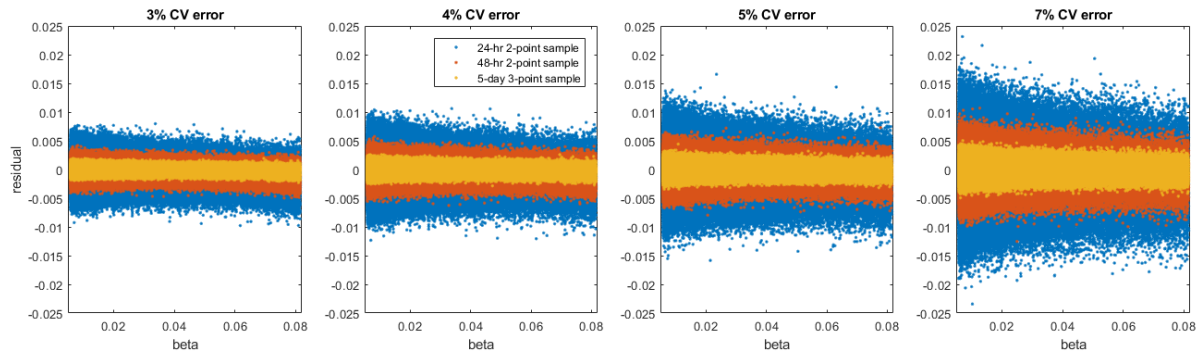


Figure 1: residual plot of  $\beta$  estimates

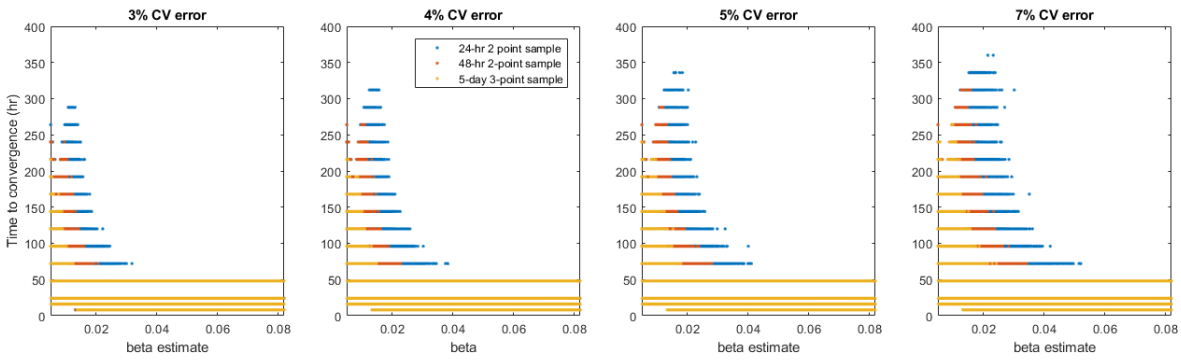


Figure 2: scatter of plot of time to convergence as a function of the estimated  $\beta$

Beta residuals x 1000				
		Sampling method		
		24 hr	48 hr	3 points
%CV error	3%	0.34 +/- 1.82	0.17 +/- 0.91	0.06 +/- 0.43
	4%	0.34 +/- 2.40	0.17 +/- 1.20	0.06 +/- 0.57
	5%	0.35 +/- 2.99	0.18 +/- 1.49	0.05 +/- 0.72
	7%	0.34 +/- 4.18	0.18 +/- 2.09	0.04 +/- 1.00

Table 1: residual error of the  $\beta$  estimates. All values were multiplied by 1000

Critical estimated T1/2 $\beta$ (hours)				
		Sampling method		
		24 hr	48 hr	3 points
%CV error	3%	56.66062	101.6738	
	4%	52.22409	82.94461	153.2405
	5%	36.35486	76.72882	143.378
	7%	31.3061	44.90001	105.2546

Table 2: Critical estimated T1/2  $\beta$  values that would lead to 0% chance of 50% overshoot.